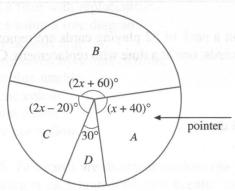
15. The face of a circular disk is divided into sectors A, B, C and D as shown in the figure below.



- (a) Find the value of x.
- (b) Which sector is the pointer least likely to indicate each time the disk is spun? Explain your answer.
- (c) The disk is spun twice and the sector that the pointer indicates is noted after each spin. Calculate the probability that the pointer
  - (i) will indicate the same sector each time,
  - (ii) will indicate a different sector each time.
- (d) Calculate the probability that the pointer will indicate the sector stated in (b) in at least one of 2 spins.
- 16. (a) A coin is drawn at random from w ten-cent coins, x fifty-cent coins and 8 one-dollar coins. The probability of drawing a ten-cent coin or a fifty-cent coin is  $\frac{1}{2}$ . The total value of all the coins is \$10.
  - (i) Form a pair of simultaneous equations involving w and x.
  - (ii) Solve the simultaneous equations to find the values of w and x.
  - (b) If instead two coins are drawn at random one at a time without replacement, calculate the probability of drawing 2 coins that is worth at least \$0.60 in total.
- 17. A clip dispenser contains m paper clips of which 6 are red and the rest are green. Two paper clips are selected at random, one at a time without replacement. The probability of selecting 2 red paper clips is  $\frac{1}{3}$ .
  - (a) Form an equation in m and show that it can be reduced to  $m^2 m 90 = 0$ .
  - **(b)** Solve the equation  $m^2 m 90 = 0$ .
  - (c) Hence, write down
    - (i) the total number of paper clips in the clip dispenser initially,
    - (ii) the number of green paper clips in the clip dispenser.
- 18. A batch of 10 components will be rejected upon first detecting a faulty component in a random test of 3 components, one after another without replacement. Suppose that there are 4 faulty components in a particular batch.
  - (a) Draw a tree diagram to represent the testing process, showing at each branch the two events: 'faulty' and 'good'.
  - (b) Hence, calculate the probability of
    - (i) rejecting the batch after testing one component,
    - (ii) rejecting the batch after testing two components,
    - (iii) not rejecting the batch.